

(Please write your Exam Roll No.)

Exam Roll No.

END TERM EXAMINATION

FIRST SEMESTER [MCA] DECEMBER-2012

Paper Code: MCA 105

Subject: Discrete Mathematics

Time: 3 Hours

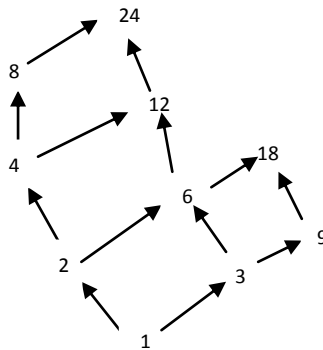
Maximum Marks: 60

**Note: Attempt any five questions including Q. no. 1 which is compulsory.
Select one question from each Unit.**

Q1 Answer the following: -

(2 x 10 = 20)

- Prove that a tree with n vertices has $n-1$ edges.
- Show that $(a-c) \cap (c-b) = \Phi$, without using Venn diagrams. Where A, B, C are non-empty sets.
- State Fermat's little theorem.
- What is the coefficient of X^8Y^9 in the expansion of $(3x+2y)^{17}$?
- Give an example of graph having Hamiltonian circuit but not an Eulerian circuit.
- If R and S are relations from A to B such that $R \subseteq S$ then prove that $R^{-1} \subseteq S^{-1}$.
- Prove that in an undirected graph numbers of odd degree vertices are even.
- Prove or disprove that $A \cup B$ is a group, where A and B are groups.
- Does the following hasse diagram represent a lattice? Give reason.



- How many solutions are there for the equation $X+Y+Z=17$, where X, Y, Z are non negative integers?

Unit -1

Q2. (a) Find the conclusion for the following hypothesis:- (5)

It is not sunny this afternoon and it is colder than yesterday

We will go swimming, only if it is sunny

If we do not go swimming, then we will take a canoe trip

If we take a canoe trip, then we will be home by sunset.

(b) Use mathematical induction to show that $H_2^n \geq 1 + n$ whenever n is a nonnegative integer.

Where $H_j = 1 + 2 + 3 + \dots + j$ (5)

Q3. (a) Let A be a set with n elements, find how many relations on A are there which (i) symmetric and (ii) anti-symmetric? (4)

(b) How many integers must you pick in order to be sure that at least two of them have the same remainder when divided by 7? (3)

(c) Use proof by cases to show that, where x and y are real numbers. (3)

Unit -2

Q4. (a) Show that every finite lattice has a least upper bound and a greatest lower bound. (5)

(b) Simplify the Boolean function $F(a, b, c, d) = \sum (0,1,2,3,4,5,7,6,8,9,11)$. (5)

Q5. (a) Minimize the following sum of product expansion: $xy\bar{z} + \bar{x}yz + \bar{x}\bar{y}z + x\bar{y}\bar{z}$. (5)

(b) Find the solution of the recurrence relation $a_n = 5a_{n-1} - 6a_{n-2} + 7^n$. Find $n \geq 2$. (5)

Unit- 3

Q6. (a) State and Prove Lagrange's Theorem for groups. (5)

(b) Find the code words generated by the parity-check matrix given below (5)

Q7. (a) Show that if a, b are arbitrary elements of a group G , then $(ab)^2 = a^2 b^2$ if G is abelian. (5)

(b) Explain Euclidean algorithm to find the gcd of two no's by taking example. (5)

Unit -4

Q8. (a) Let G be a connected planar simple graph with E is number of edges and V is number of vertices and R is a number of regions then $V-E+R = 2$. (5)

(b) State and prove five-color theorem for graphs. (5)

Q9. (a) Write a short note on Seven Bridge Problem of graph theory. (5)

(b) Define pre order and post order traversal of a tree. Determine the order in which a preorder and post order traversal visits the vertices of the following ordered rooted tree. (5)