

(Please write your Exam. Roll No.)

Exam. Roll No. 084

# END TERM EXAMINATION

FOURTH SEMESTER [BCA], MAY - 2011

Paper Code : BCA 202

Subject : Mathematics-IV

Paper Id : 20202

Time : 3 Hours

Maximum Marks : 75

Note : Q.No.1 is compulsory. Attempt One question from each unit.

Q. 1 (a) An urn contains 10 black and 10 white balls. Two balls are drawn from it. Find the probability that the two balls are of the same colour.  $(10 \times 2.5 = 25)$

(b) Find n if  $P(n, 4) = 42 P(n, 2)$ .

(c) Let  $\Delta$  and  $\nabla$  denote respectively the first forward and first backward difference operators. Prove that  $\Delta \nabla = \Delta - \nabla$ .

(d) Suppose X is a Poisson variate. If  $P(X=1) = 2 P(X=2)$ , find  $P(X=0)$ .

(e) The two regression coefficients are  $-0.1$  and  $-0.9$ . Find r, the coefficient of correlation.

(f) Find the probability of getting 4 heads in 6 tosses of an unbiased coin.

(g) In how many ways can 6 boys be arranged along the boundary of a circle.

(h) Construct forward difference table from the values of x and y given below

x	0	1	2	3	4	5
y	5	11	22	18	27	2

From the table, write the values of  $\Delta^2 y_3$ ,  $\Delta^3 y_2$  and  $\Delta^4 y_1$ .

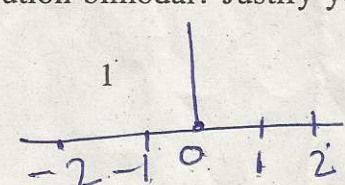
(i) Evaluate  $\int_{-2}^2 x^3 dx$ , using Trapezoidal rule, by dividing the closed interval  $[-2, 2]$  into 4 equal parts.

(j) Consider a binomial distribution with parameters  $n=8$  and  $p=\frac{1}{2}$ . Is this binomial distribution bimodal? Justify your answer.

15  
4  
5  
5  
-----  
15  
10  
4  
29

$\frac{2+2}{4} = \frac{4}{4} = 1$

-2  
-2, -1, 0, 1, 2  
-2 + 1  
= -1



P.T.O.



UNIT-I

Q. 2. (a) Find the probability of getting the sum 10 in one throw with three dice. (6)

(b) If A and B are independent events and  $P(A) = P(B/A) = \frac{1}{2}$ , find  $P(A \cup B)$ . (6.5)

6

~~$P(B/A) = \frac{P(A \cap B)}{P(A)}$~~   
 $\frac{1}{2} = \frac{P(A \cap B)}{\frac{1}{2}} \Rightarrow P(A \cap B) = \frac{1}{4}$

Q. 3. (a) Out of  $(2n+1)$  tickets consecutively numbered, three tickets are drawn at random. Find the probability that the numbers on these three tickets form an arithmetic progression. (6.5)

$\frac{1}{2} + \frac{1}{2} = 1$   
 $\frac{1}{2} + \frac{1}{2} = 1$   
 $\frac{1}{2} + \frac{1}{2} = 1$   
 $\frac{1}{2} + \frac{1}{2} = 1$

(b) An urn A contains 'a' white and 'b' black balls. Another urn B contains 'c' white and 'd' black balls. One ball is transferred from the urn A into the urn B and then a ball is drawn from the urn B. Assuming that the ball drawn is white, find the probability that the transferred ball was also white. (6)

UNIT-II

Q. 4. (a) Find the constant c for which  $ce^{-2x^2+x}$ ,  $-\infty < x < \infty$ , is a normal density function of a real-valued continuous random variable. (6)

(b) Given the lines of regression  $2x - 9y + 6 = 0$  and  $x - 2y + 1 = 0$ , determine the means  $\bar{x}, \bar{y}$  and the regression coefficients  $b_{xy}, b_{yx}$ . Also, find the coefficient of correlation between x and y. (6.5)

Q. 5. (a) The data given below indicate the marks obtained out of 30 in the written tests conducted in Statistics and Economics. Compute Spearman's rank correlation coefficient :



Students	Marks in Statistics (x)	Marks in Mathematics (y)
A	20	18
B	18	16
C	26	29
D	15	27
E	17	12

4

(6)

1

- (b) Define the Karl Pearson Coefficient of correlation between the variates X and Y. Compute it from the data given below :

$$\text{Cov}(X, Y) = 15.4, \quad \sigma_x = 6, \quad \sigma_y = 7$$

(3.5)

- (c) Suppose X is a normal variate with mean  $\mu = 0$  and variance  $\sigma_x^2 = 1$ . Find  $E(|X|)$ , the expected value of the variate  $|X|$ .

(3)

### UNIT-III

- Q. 6. (a) By using Newton's forward interpolation formula, find the cubic polynomial which can be fitted by using the following data :

5

x	0	1	2	3
f(x)	1	2	1	10

(5)

- (b) By using Bijection method, find a positive root of the equation  $x e^x - 1 = 0$ , correct to three decimal places, using the fact that  $f(0)$  and  $f(1)$  are of opposite signs where  $f(x) = x e^x - 1$ .

(7.5)

- Q. 7. (a) Given  $\sqrt{5} = 2.236$ ,  $\sqrt{6} = 2.449$ ,  $\sqrt{7} = 2.646$  and  $\sqrt{8} = 2.828$ , find the value of  $\sqrt{5.5}$  by using Newton's forward interpolation formula.

(6)

- (b) By using Newton-Raphson method, find a positive root of the equation  $x e^x - 1 = 0$ . Use the fact that  $f(0)$  and  $f(1)$  are of opposite signs where  $f(x) = x e^x - 1$ . Start with  $x_0 = 0.5$  and perform only two iterations.

(6.5)



**UNIT-IV**

**Q. 8. (a)** Find the  $[U]$  decomposition of the matrix  $A = \begin{pmatrix} 2 & 3 & 1 \\ 1 & 2 & 3 \\ 3 & 1 & 2 \end{pmatrix}$  **(6)**

**(b)** By using Gauss elimination method, solve the following system of linear equations :

$$6x - y - z = 19$$

$$3x + 4y + z = 26$$

$$x + 2y + 6z = 22$$

**(6.5)**

**Q. 9. (a)** By using Gauss-Jordan method, solve the following system of linear equations :

$$2x + y + z = 10$$

$$3x + 2y + 3z = 18$$

$$x + 4y + 9z = 16$$

**(6)**

**(b)** Determine the actual value of the integral  $\int_0^1 \frac{1}{1+x^2} dx$ . Also,

16 evaluate this integral, using Simpson's  $\frac{1}{3}$ rd rule, by dividing the interval  $[0, 1]$  into four equal parts. Compare the two values, so obtained, of the integral under consideration, and find an approximate value of  $\pi$ . **(6.5)**

6  
6  
5  
5  
~~5~~

25 - 24  
20

15  
12  
10  

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6  
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26  
24  

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50